Mathematics 3271 3.0 Fall 2017 Assignment 1

1. Section 14 in Weinberger: 1(a)

2. Let f be a nonzero continuous function on the boundary ∂D of the square $D = \{(x, y) \in \mathbb{R}^2 : 0 \le x, y \le \pi\}$ such that f is equal to 0 at the four vertices. Find a continuous solution u on D of the Dirichlet problem

$$\left\{ \begin{array}{ll} \frac{\partial^2 u}{\partial x^2} + \frac{\partial^2 u}{\partial y^2} = 0, \qquad (x,y) \in \{(x,y) \in \mathbb{R}^2 : 0 < x, y < \pi\} \\ u(x,y) = f(x,y), \qquad (x,y) \in \partial D. \end{array} \right.$$

3. Section 15 in Weinberger: 1, 3, 5

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